

# Magnetization Dynamics under Heat Currents

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# Spintronics Group members

## Post-docs

- Sylvain Bréchet, *theory*
- Pedro Saraiva *ESR*

## Present and recent grad students

- Elisa Papa, *FMR in SSE geometry*
- Antonio Vetro *time resolved FMR*
- F. Comandè *spin-dependent charge recombination in OLED*
- Arndt von Bieren *Nernst imaging of magnetization domains*

## Collaborations

- S. Barnes, U. Miami, Florida
- J. Barnas, J. Dubowik, T. Stobiecki

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Swiss NSF,  
SpinCat, DFG

Nanospin : joint research programs with Poland



# Outline

- The magnetic Seebeck effect (insulator)
- Heat-driven spin current in spin valves (metals)
  - switching in spin valves
  - linear response of spin valves to heat-driven spin currents

# A magnetic Seebeck effect

PRL **111**, 087205 (2013)

PHYSICAL REVIEW LETTERS

week ending  
23 AUGUST 2013



## **Evidence for a Magnetic Seebeck Effect**

Sylvain D. Brechet,<sup>1,\*</sup> Francesco A. Vetro,<sup>1</sup> Elisa Papa,<sup>1</sup> Stewart E. Barnes,<sup>2</sup> and Jean-Philippe Ansermet<sup>1</sup>

# Thermodynamics with electromagnetic fields

## Publications

### Articles

S. Bréchet, A. Vetro, E. Papa, S. Barnes and J.-P. Ansermet. *Evidence for a Magnetic Seebeck Effect*, in Physical Review Letters, vol. 111, num. 8, p. 087205, 2013.

[Détails](#) - [Full Text](#) - [Version de l'éditeur](#)

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S. Bréchet, A. Roulet and J.-P. Ansermet. *Magnetoelectric Ponderomotive Force*, in Modern Physics Letters B, vol. 27, num. 21, p. 1350150, 2013.

[Détails](#) - [Full Text](#) - [Version de l'éditeur](#)

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S. Bréchet and J.-P. Ansermet. *Thermodynamics of a continuous medium with electric and magnetic dipoles*, in European Physical Journal B Condensed Matter Physics, vol. 86, p. 318, 2013.

[Détails](#) - [Full Text](#) - [Version de l'éditeur](#)

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S. Bréchet and J.-P. Ansermet. *Thermodynamics of continuous media with intrinsic rotation and magnetoelectric coupling*, accepted in Continuum Mechanics and Thermodynamics, p. 1-28, 2013.

[Détails](#) - [Full Text](#) - [Version de l'éditeur](#)

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S. Bréchet, F. Reuse and J.-P. Ansermet. *Thermodynamics of continuous media with electromagnetic fields*, in European Physical Journal B Condensed Matter Physics, vol. 85, p. 412, 2012.

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**Sylvain Bréchet**

[sylvain.brechet@epfl.ch](mailto:sylvain.brechet@epfl.ch)

<http://moodle.epfl.ch/course>

- **Thermostatistics**

$$u = T s - P + \sum_A \left( \mu_A + q_A V - \mathbf{m}_A \cdot \mathbf{B} \right) n_A$$

- **Reversible thermodynamics**

$$\mathbf{j}_u = T \mathbf{j}_s + \sum_A \left( \mu_A + q_A V - \mathbf{m}_A \cdot \mathbf{B} \right) \mathbf{j}_A$$

- **Irreversible thermodynamics**

$$\rho_s = \frac{1}{T} \left\{ \sum_a \omega_a \mathcal{A}_a + \sum_A \Omega_A \cdot \left( \mathbf{m}_A \times \mathbf{B} \right) + \mathbf{j}_s \cdot \left( -\nabla T \right) \right. \\ \left. + \sum_A \mathbf{j}_A \cdot \left( -\nabla \mu_A - q_A \nabla V - m_A \mathbf{v}_A \nabla \mathbf{v} + \mathbf{m}_A \nabla \mathbf{B} \right) \right\}$$

# Relationships between currents and generalized forces

- Lehman effect
- Debye relaxation of electric dipoles
- Landau-Lifshitz with damping
- Coupling current of magnetic dipoles and magnetization
- Coupling heat current of metals and magnetization

**Linear relation :** (Eur. Phys. J. B 86, 318 (2013))

- $\mathbf{j}_e = L_{es} \cdot (-\nabla T) + L_{ee} \cdot (-\nabla \mu - e \nabla V + \mathbf{m} \nabla \mathbf{B})$

**Material : YIG (insulator)**

- $\mathbf{j}_e = \mathbf{0}$  (no electronic transport)
- $\nabla V = \mathbf{0}$  (no charge accumulation)
- $\nabla \mu = \mathbf{0}$  (uniform spatial distribution)

**Stationary state :**

- $\mathbf{M} \nabla \mathbf{B} = \lambda n k_B \nabla T$  where  $\mathbf{M} = n \mathbf{m}$  and  $\lambda > 0$



## Bulk identity :

- $\mathbf{M} \nabla \mathbf{B} = \mathbf{j}_M \times \mathbf{B}$     where     $\mathbf{j}_M = \nabla \times \mathbf{M}$

## Magnetic Seebeck effect

- $\mathbf{B} = \boldsymbol{\varepsilon}_M \times \nabla T$     where     $\boldsymbol{\varepsilon}_M = -\lambda n k_B (\nabla \times \mathbf{M})^{-1}$

## Linearisation :

- $\mathbf{B}_{\text{ext}} = \mathbf{B}_0 + \mathbf{b}$
- $\mathbf{M} = \mathbf{M}_S + \mathbf{m}$  where  $\mathbf{m} \ll \mathbf{M}_S$

## Eigenmodes :

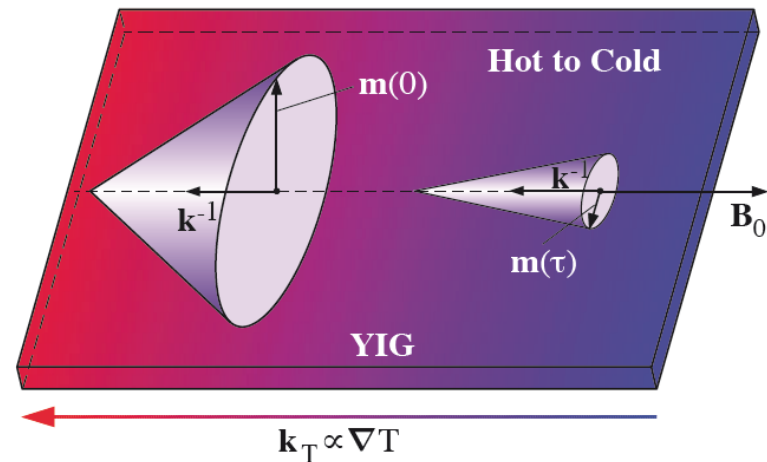
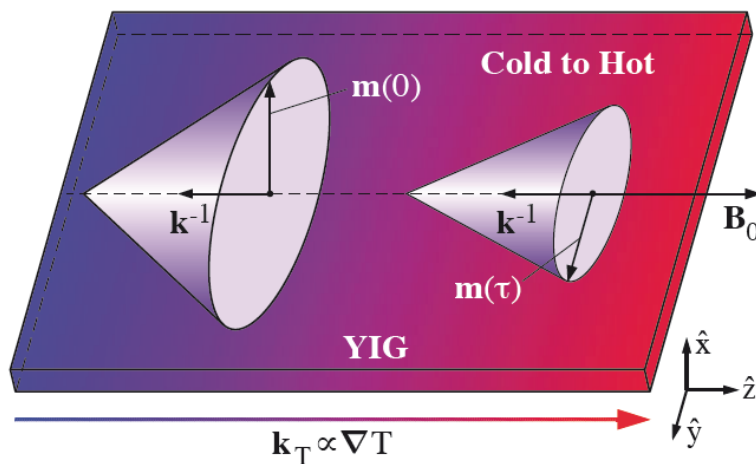
- $\mathbf{m}_{\mathbf{k}x,y} = \chi_{\mathbf{k}x,y} \mathbf{b}_{\mathbf{k}}$

- $$\chi_{\mathbf{k}x,y} = - \frac{1}{\Omega - \sqrt{\Omega_0 (\Omega_0 + 1)} + i r_{x,y} (\alpha \Omega + \mathbf{k}_T \cdot \mathbf{k}^{-1})}$$

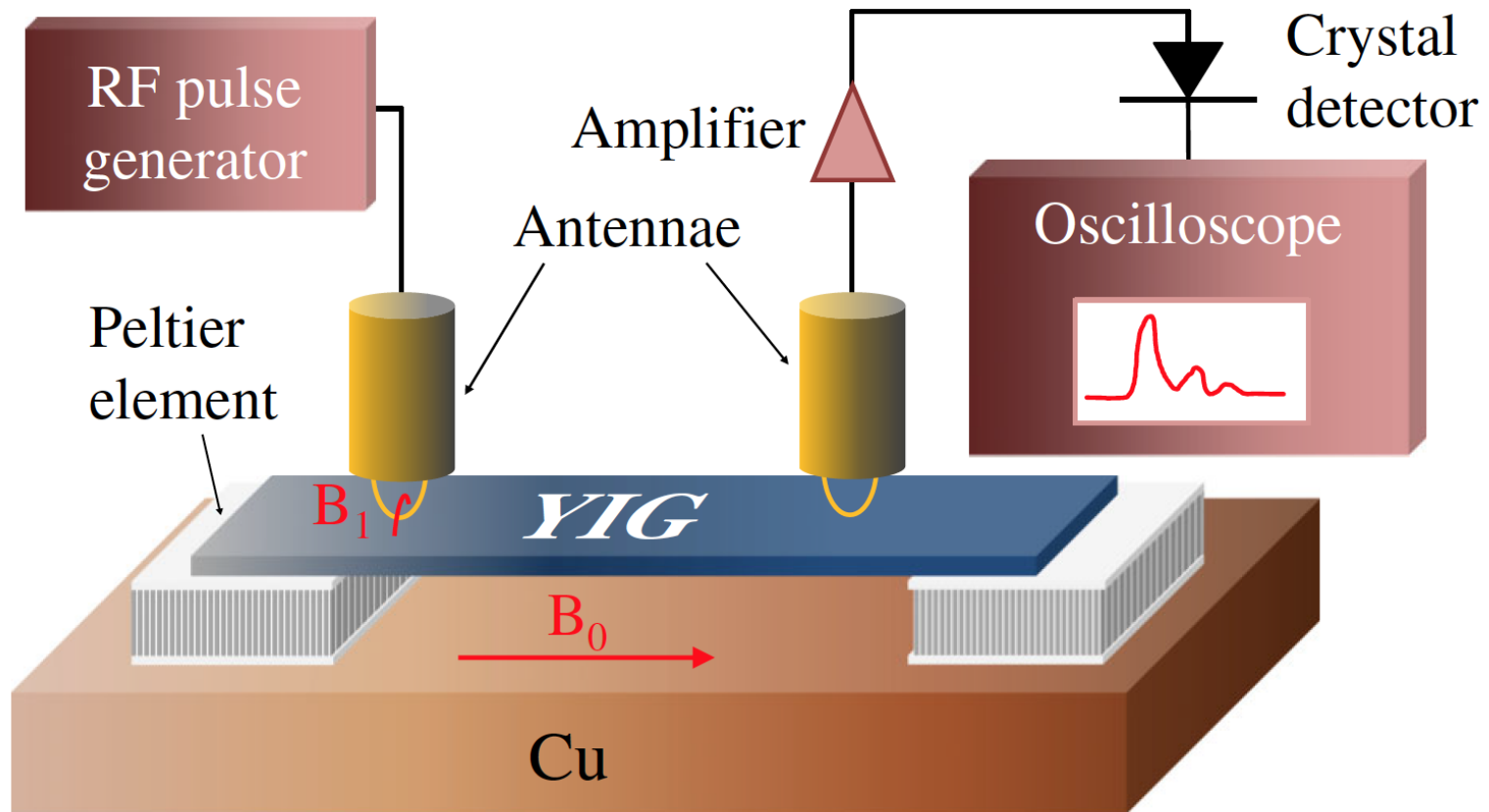
$$\Omega = \frac{\omega}{\gamma \mu_0 M_S}, \quad \Omega_0 = \frac{\gamma B_0}{\gamma \mu_0 M_S}, \quad \mathbf{k}_T = \frac{\lambda n k_B}{\mu_0 M_S^2} \nabla T$$

## Magnetisation waves propagation (YIG) :

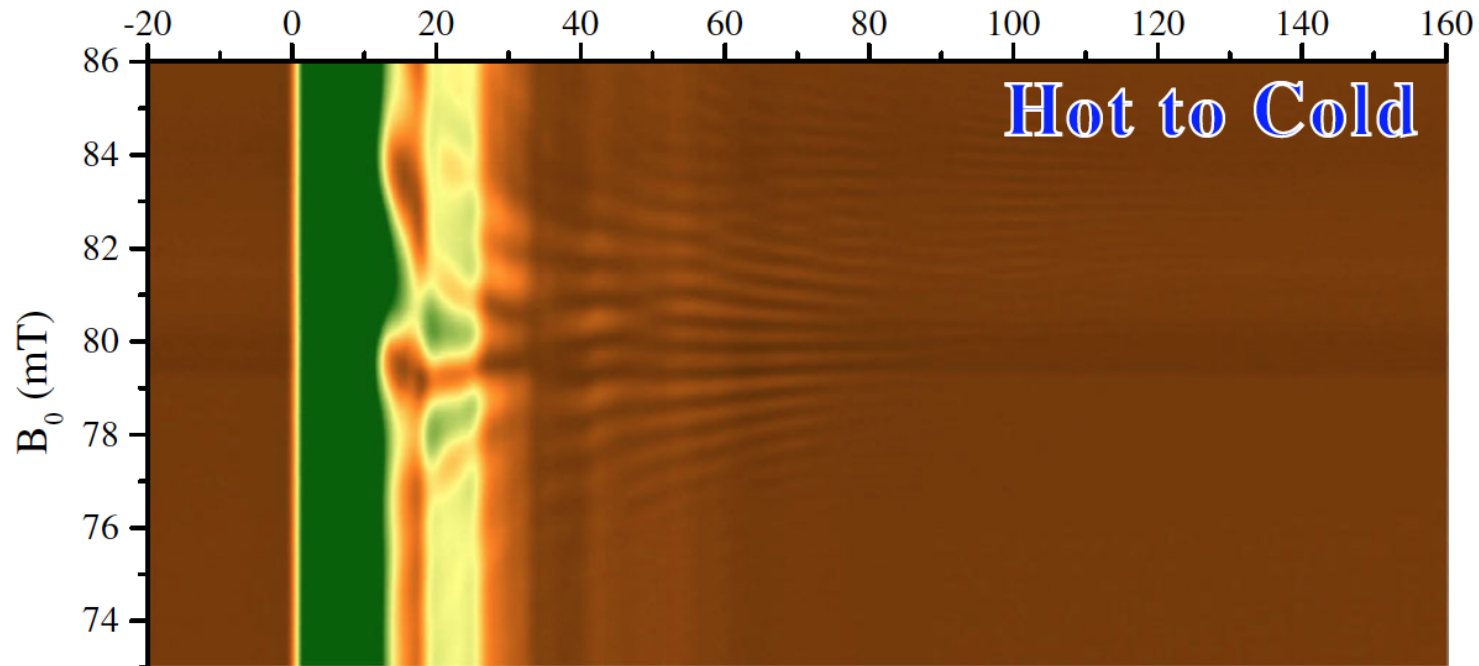
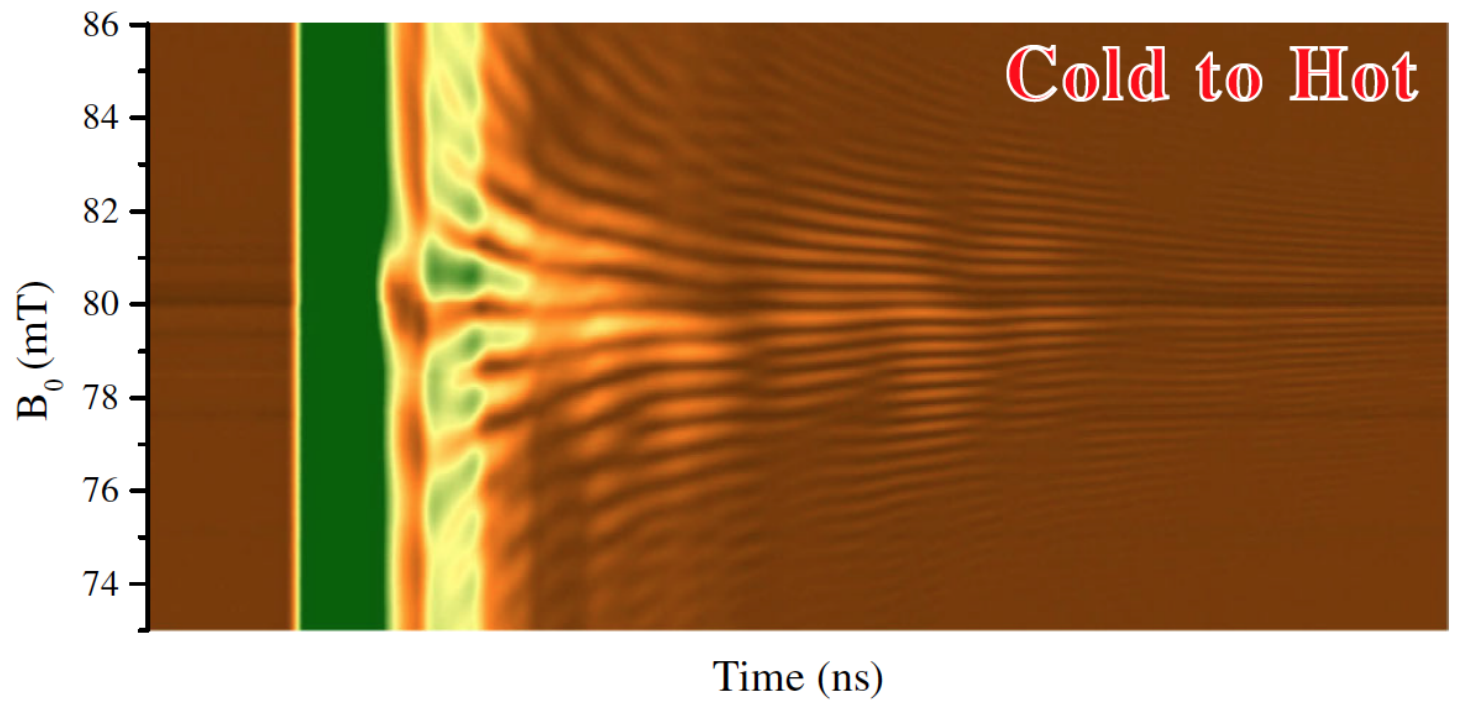
- Magnetostatic backward volume modes
- **Cold to Hot** : negative thermal damping ( $\mathbf{k}_T \cdot \mathbf{k}^{-1} < 0$ )
- **Hot to Cold** : positive thermal damping ( $\mathbf{k}_T \cdot \mathbf{k}^{-1} > 0$ )

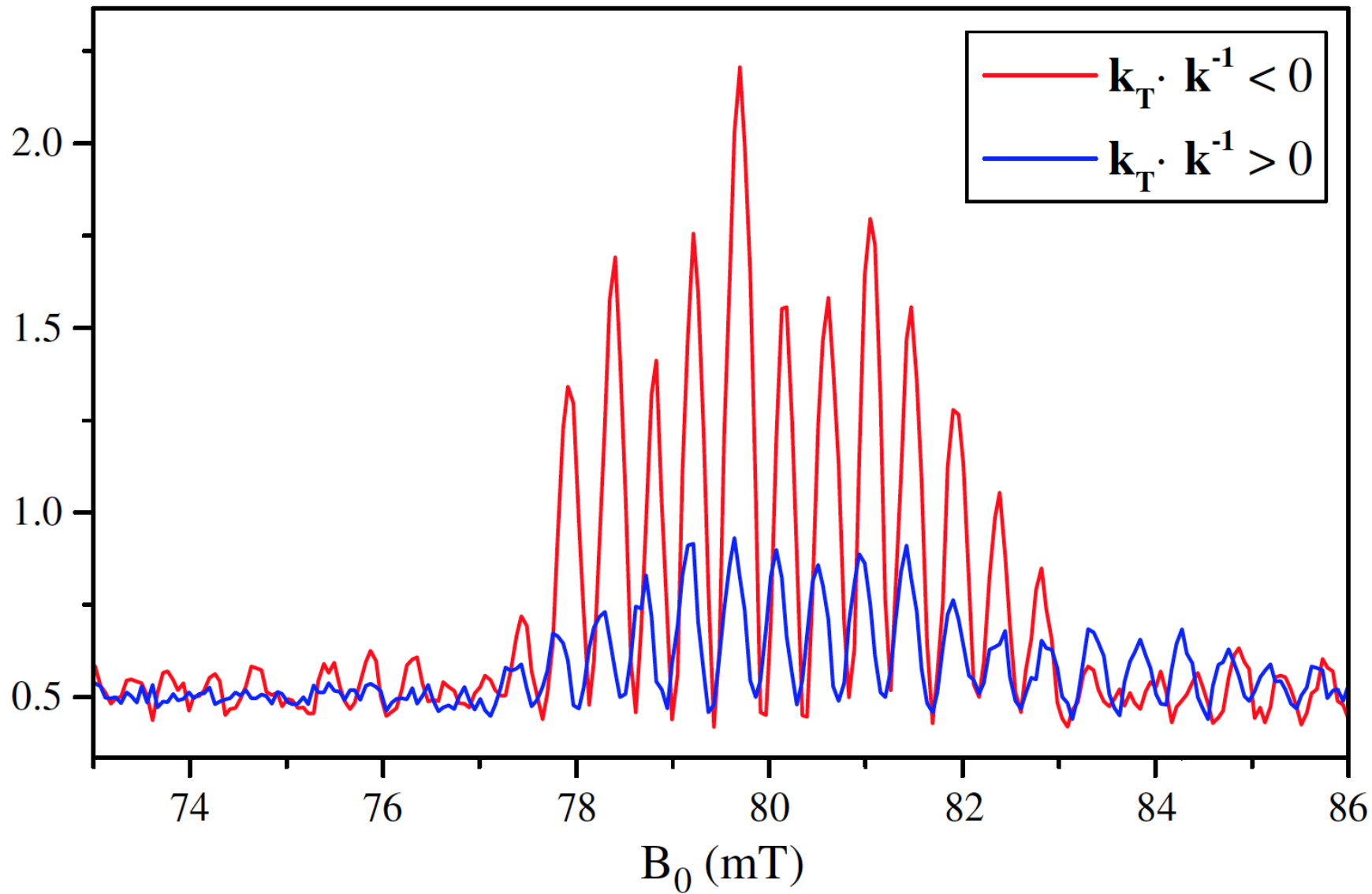


# Time resolved FMR with temperature gradient



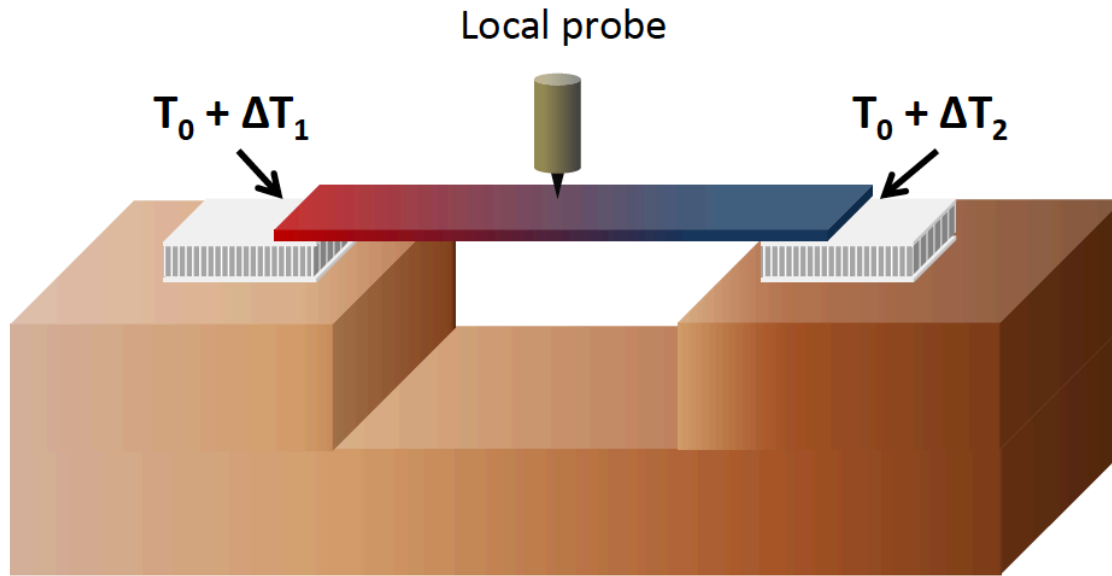
- YIG : 50 micron thick, on sapphire substrate, 7 mm long
- two Peltier elements, on heat-sinking block





Signal detected 70 ns after a 15 ns pulse at 4 GHz.

# CW studies

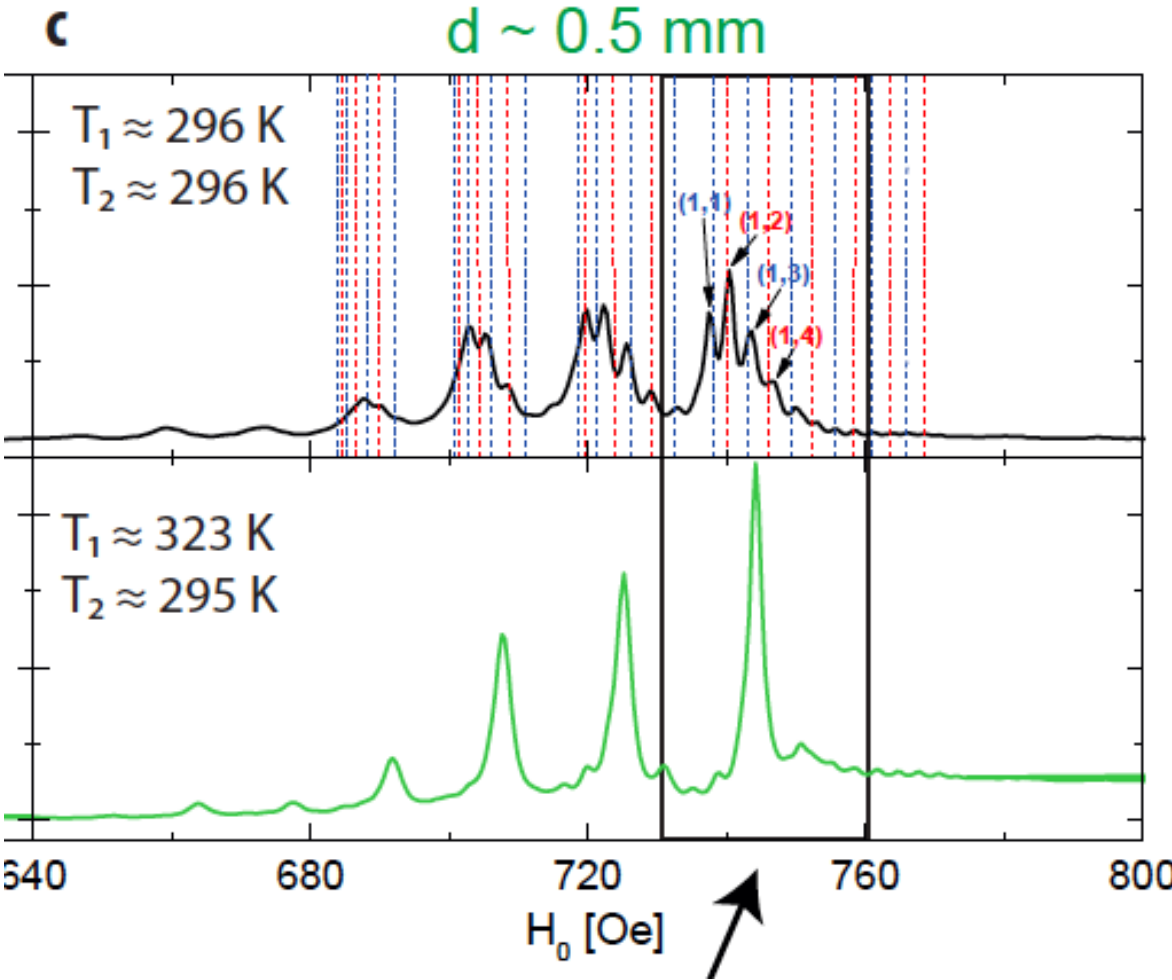


YIG :

- 50 micron thick
- on sapphire substrate, 7 mm long
- two Peltier elements
- heat-sinking block



# CW - FMR

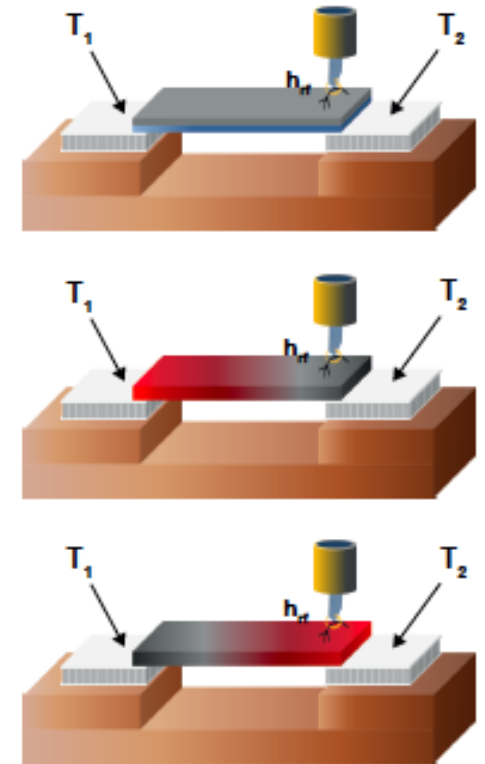
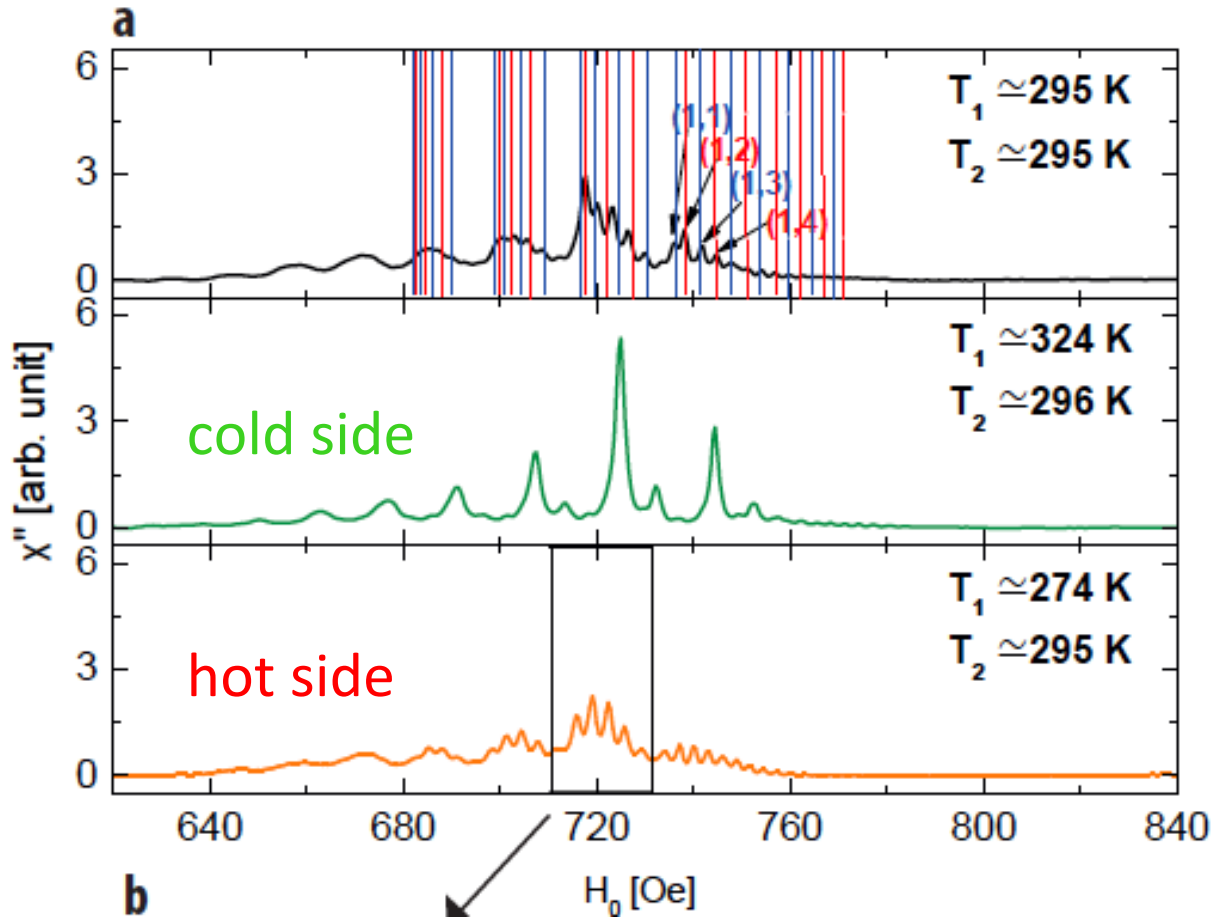


isothermal

cold side, same temperature



# No effect on the hotter side



# Heat-driven spin currents in metallic spin valves

# Three-current model

$$\begin{pmatrix} \dot{j}_s \\ j \\ \dot{j}_p \end{pmatrix} = - \begin{pmatrix} \kappa & q\sigma\epsilon & q\sigma_p\epsilon_p \\ \sigma\epsilon & \sigma & \sigma_p \\ \sigma_p\epsilon_p & \sigma_p & \sigma \end{pmatrix} \begin{pmatrix} \nabla T \\ \nabla V \\ \nabla(\Delta\mu)/q \end{pmatrix}$$

$$\sigma_{\pm} = \frac{\sigma}{2}(1 \pm \beta) \quad \epsilon_{\pm} = \epsilon(1 \pm \eta)$$

Bulk spin current in metal at zero charge current :

$$j_p = -\sigma(\eta - \beta)\epsilon\nabla T$$

L. Gravier et al, PRB 2006

S. Brechet, J.-Ph. A., phys. Stat. Solidi 2010

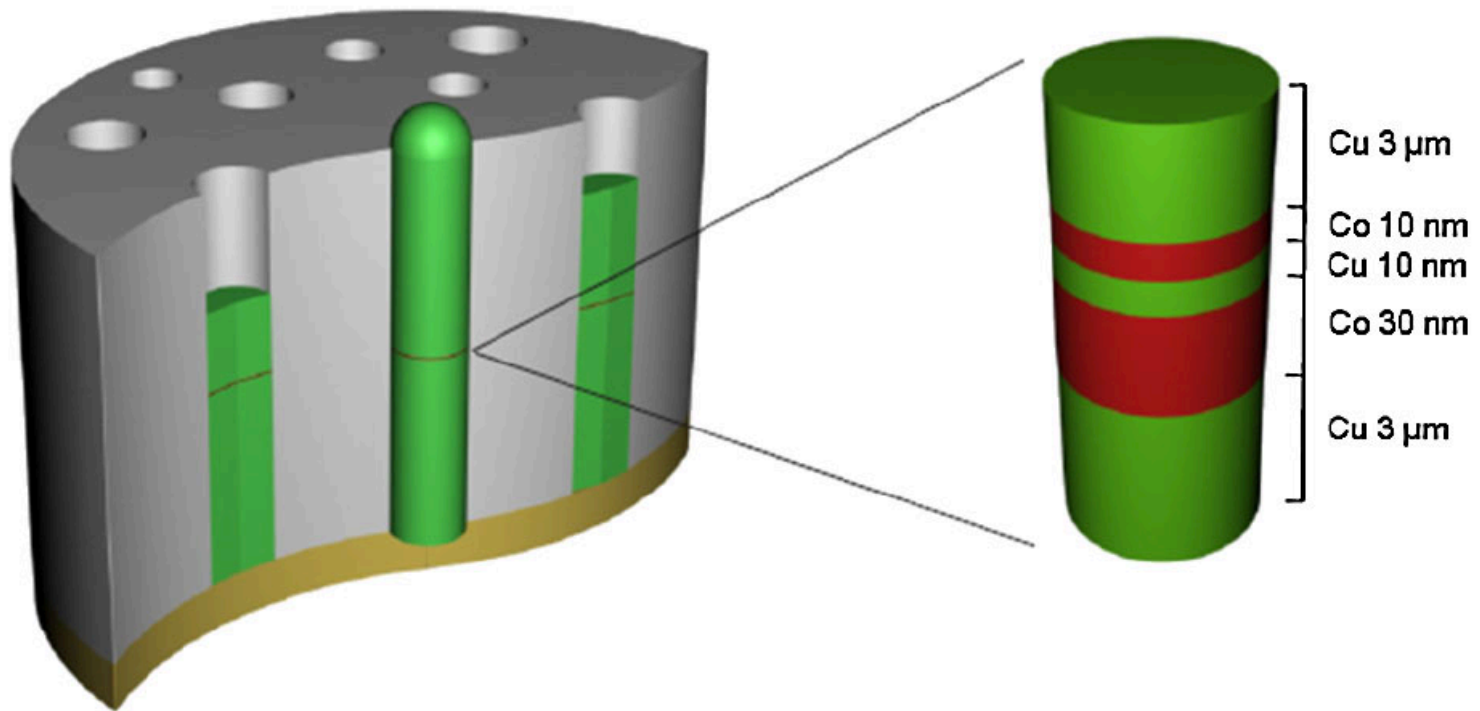
Also Sachter et al., Nat. Phys. 2010

## Evidence for Thermal Spin-Transfer Torque

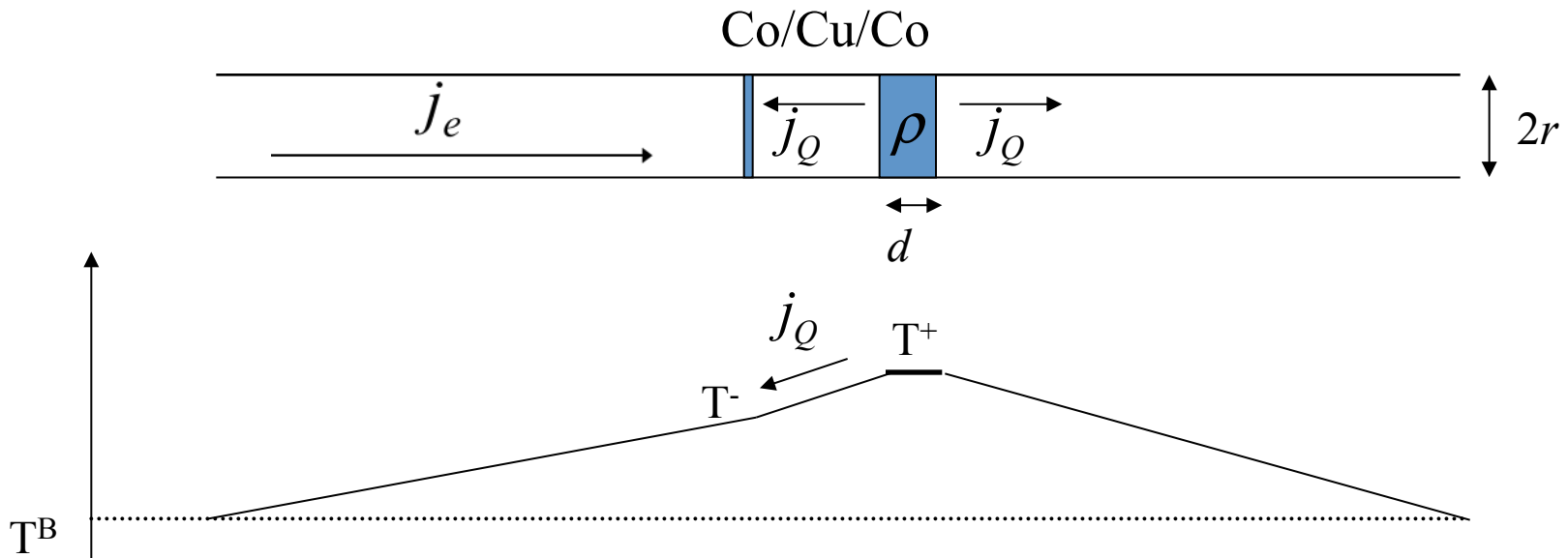
Haiming Yu,<sup>1,2</sup> S. Granville,<sup>1</sup> D. P. Yu,<sup>2</sup> and J.-Ph. Ansermet<sup>1</sup>

<sup>1</sup>*Ecole Polytechnique Fédérale de Lausanne, IPMC, Station 3, CH-1015 Lausanne-EPFL, Switzerland*

<sup>2</sup>*State Key Laboratory for Mesoscopic Physics, School of Physics, Peking University, Beijing 100871, People's Republic of China*



# Joule heating spin valves in a nanowire



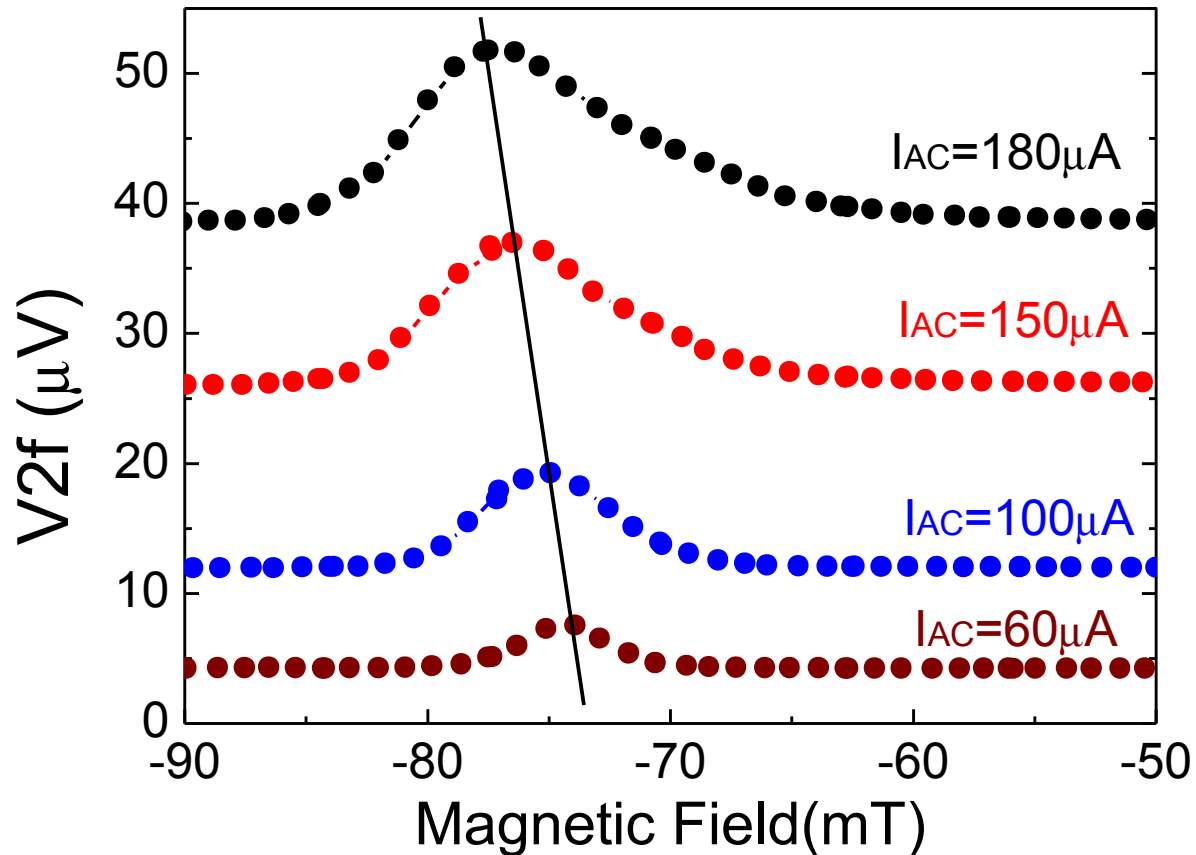
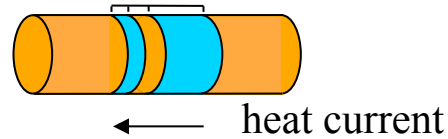
$$\nabla T \approx 10'000 K / cm$$

$$\Delta T < 1 K$$

$$\frac{1}{2} \rho \frac{d}{\pi r^2} I^2 = j_Q \pi r^2 \quad \longrightarrow \quad j_Q \propto \frac{1}{r^4}$$

Nanowires **ideal** for large  $j_Q$

# Heat current (not temperature) changes the switching field



NB : reversible, no minor loop in field

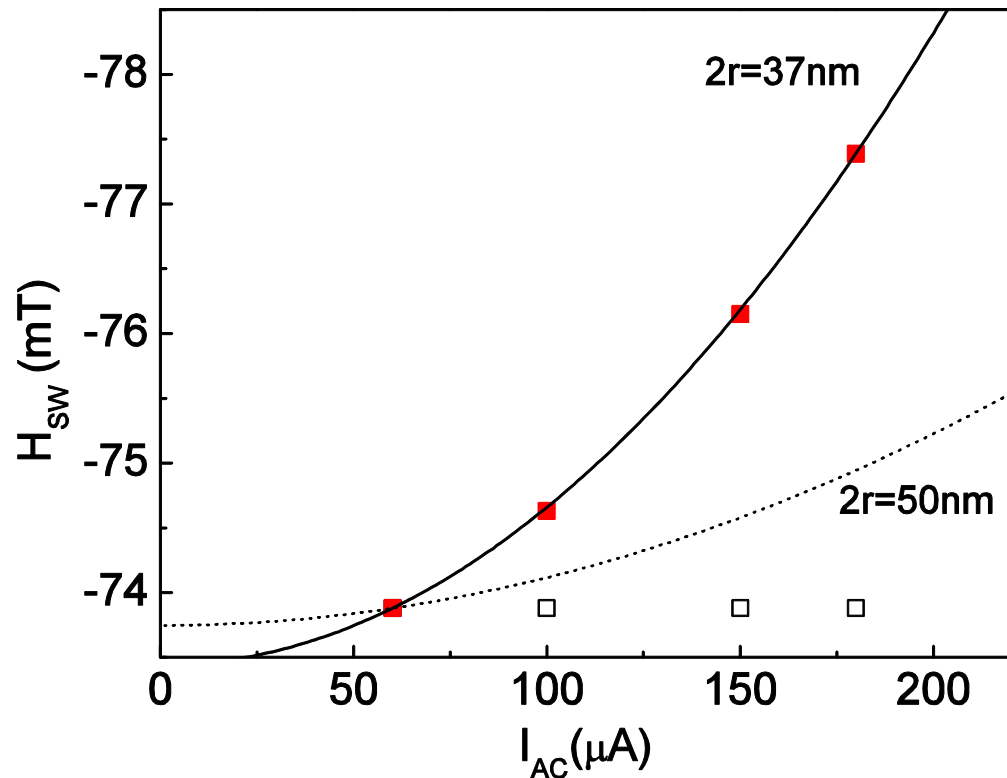
$I_{dc} = 0.1 \text{ mA}$

# Heat-current and charge-current driven spin torques compared :

$$j_p = c(\nabla V - S_{eff} \nabla T)$$

$$\frac{\Delta H_{sw}^{TST}}{\Delta H_{sw}^{STT}} = \frac{\tau_{TST}}{\tau_{STT}} = \frac{j_{p,TST}}{j_{p,STT}} = \frac{S_{eff} \nabla T}{\nabla V}$$

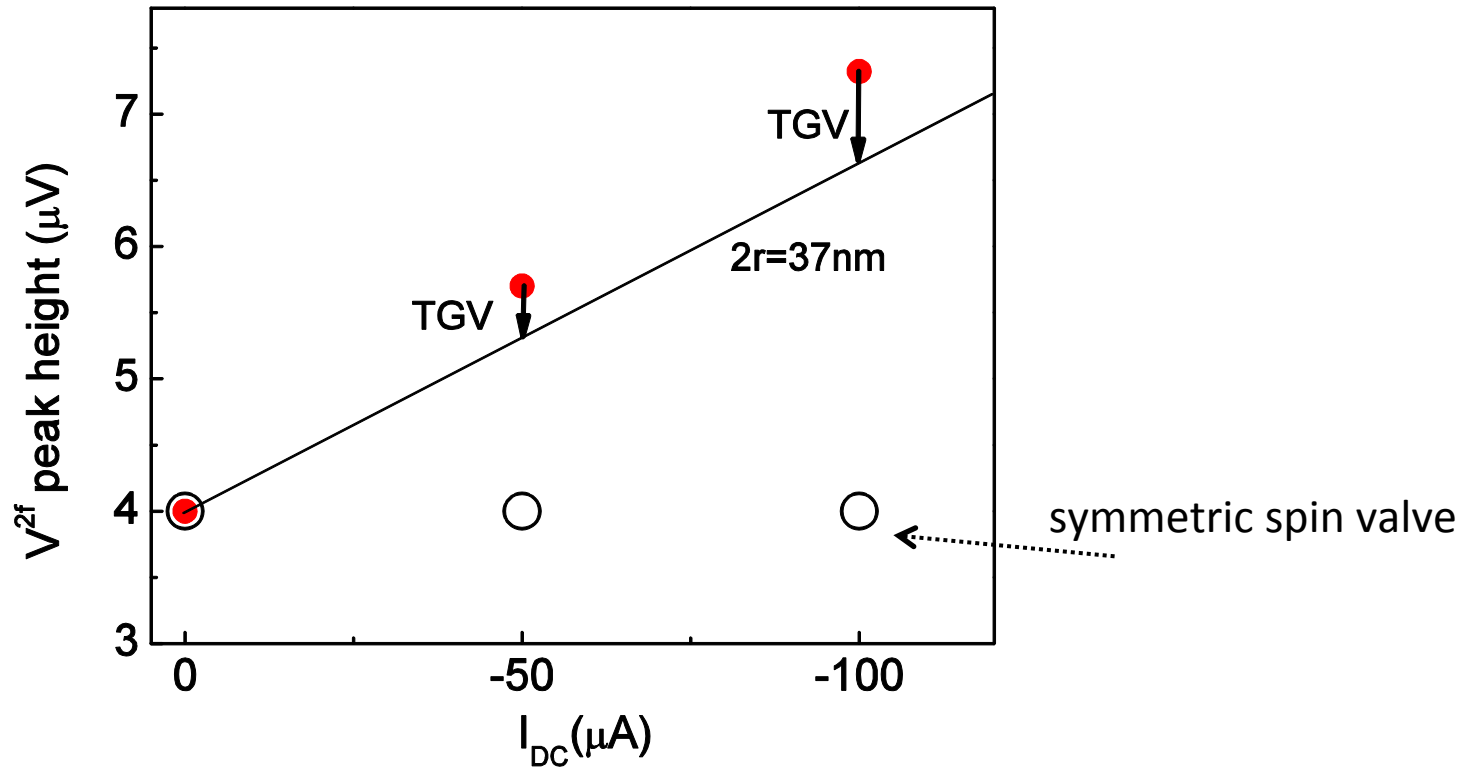
From 3-current model,  
values measured independently



STT effect of  $I_{dc}$  :

H. Yu, J. Dubois, ..., J.-Ph. A.,  
J. Phys. D 42, 175004 (2009).

# Independent check : peak height vs. $I_{DC}$

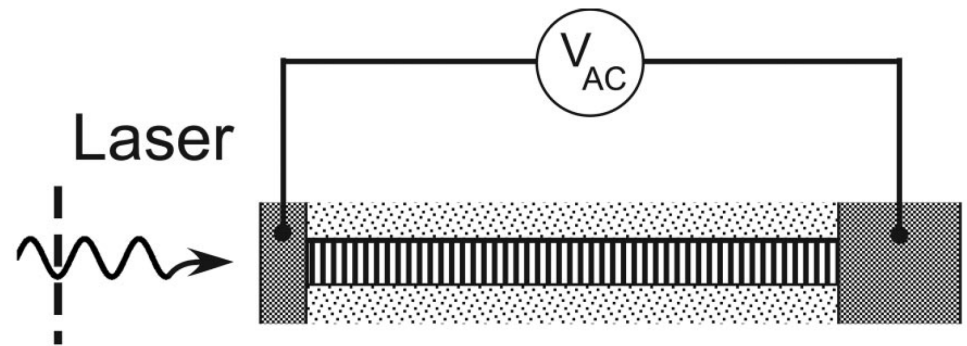
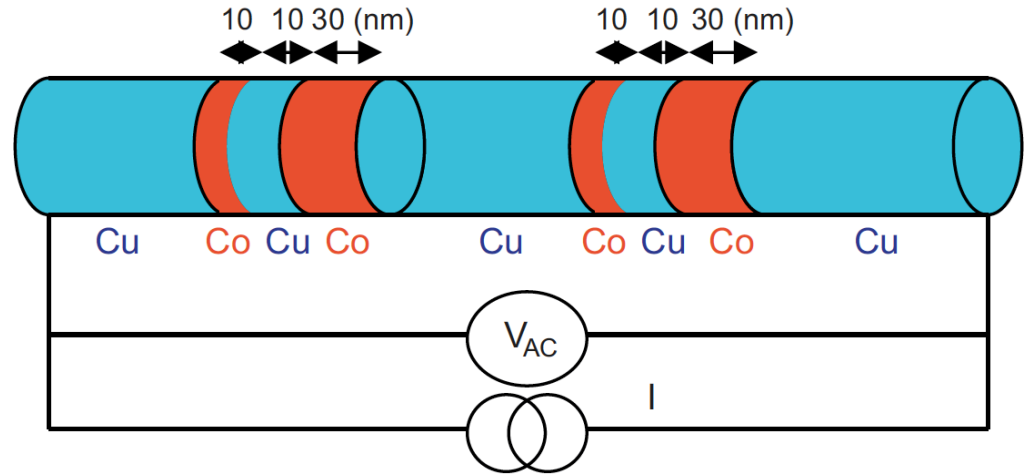


$$V_{peak}^{2f} = \left( \frac{\partial R}{\partial \tau} \frac{\partial \tau}{\partial j_m} 2c \left( \rho \frac{I_{AC}^2}{\pi r^2} + 3S_{eff} A_1 I_{DC} I_{AC}^2 \right) \right) + \frac{\partial R}{\partial T} \Delta T^{2f} I_{DC}$$



Heat-driven spin current  
in metallic spin valves :  
Linear response

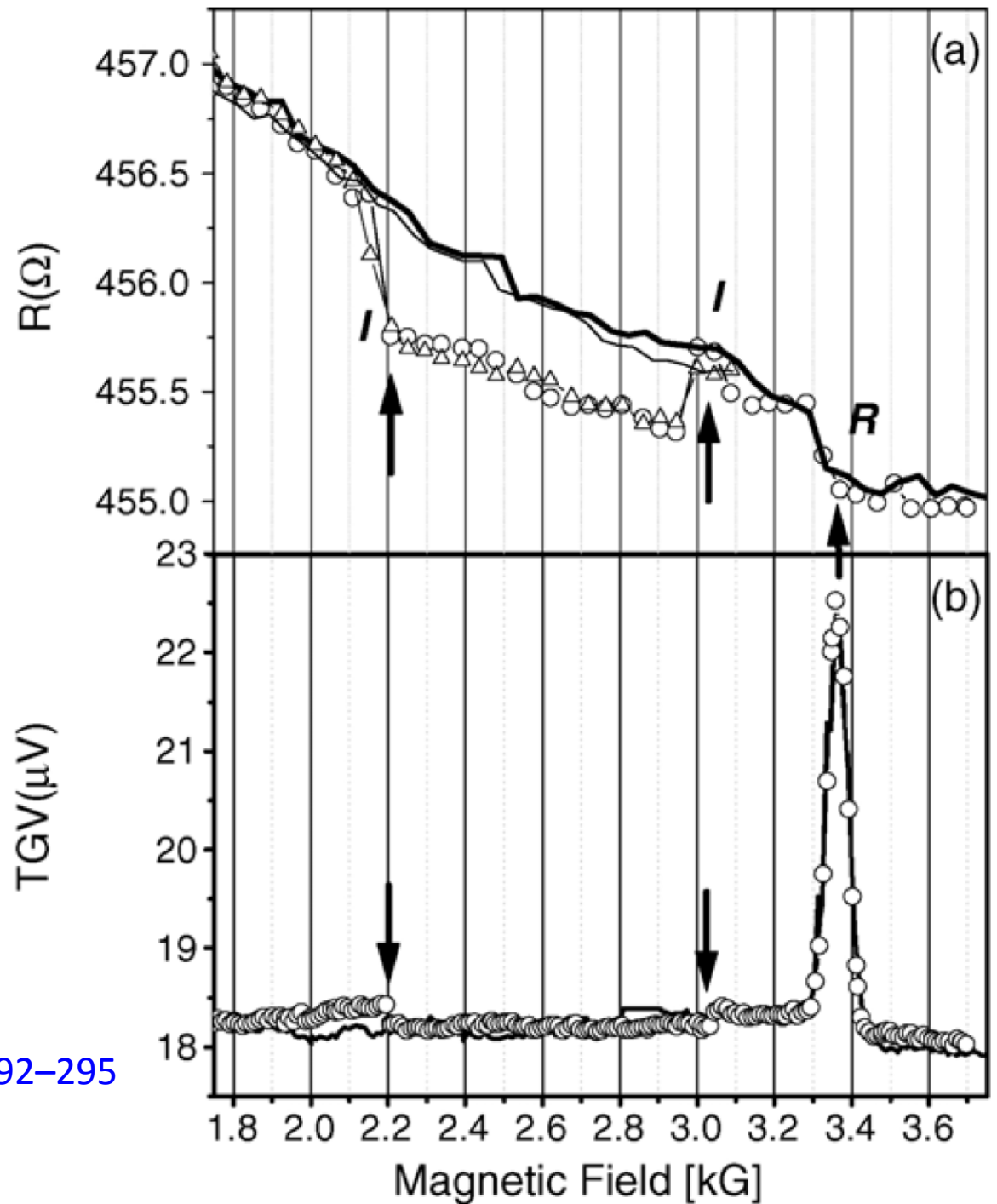
Co/Cu spin valves  
stacked  
in a nanowire



Temperature gradient about  $10^4$  K/cm

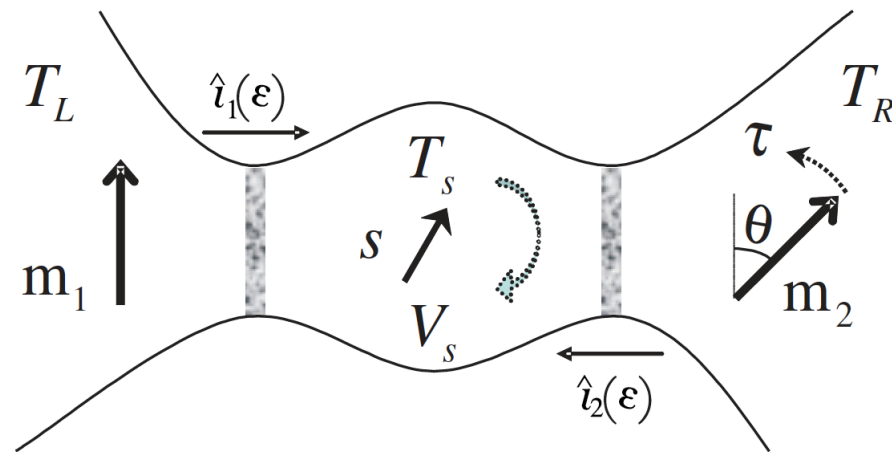
Gravier 2004

Co/Cu spin valves  
stacked  
in a nanowire



Serrano-Guisan  
Mat. Sc. and En. B 126 (2006) 292–295

# Other experiments on magnetization dynamics under heat current

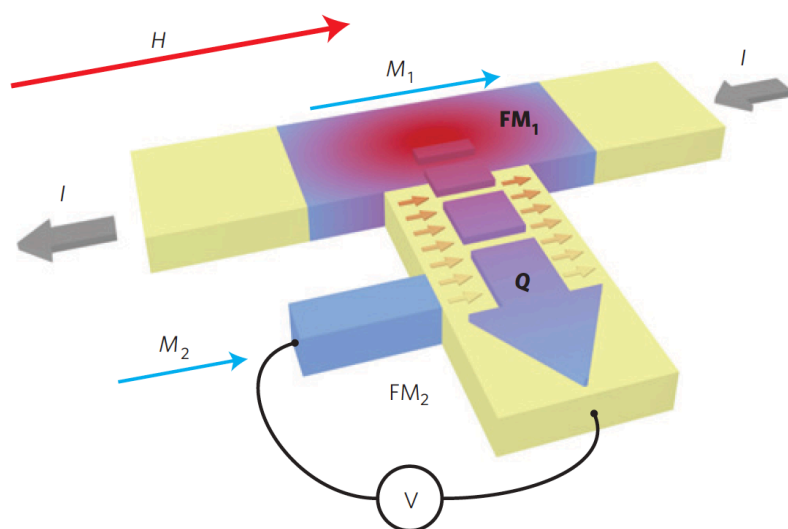


M. Hatami, G.E.W. Bauer, Q. Zhang, P.J. Kelly,  
Phys. Rev. Lett. 99, 066603 (2007)

# Thermally driven spin injection from a ferromagnet into a non-magnetic metal

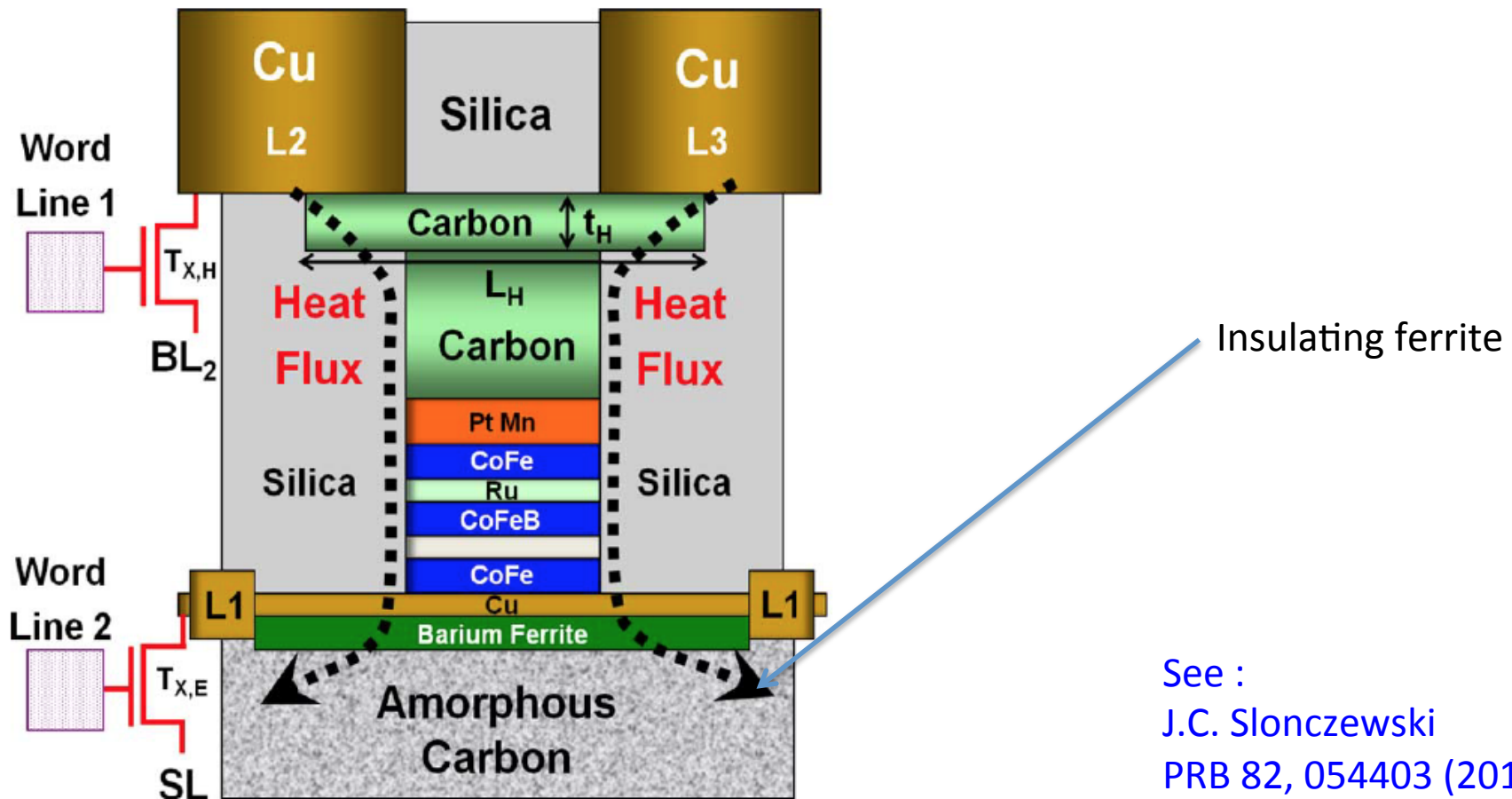
A. Slachter<sup>\*</sup>, F. L. Bakker, J-P. Adam and B. J. van Wees

$$\begin{pmatrix} J_{\uparrow} \\ J_{\downarrow} \\ Q \end{pmatrix} = - \begin{pmatrix} \sigma_{\uparrow} & 0 & \sigma_{\uparrow} S_{\uparrow} \\ 0 & \sigma_{\downarrow} & \sigma_{\downarrow} S_{\downarrow} \\ \sigma_{\uparrow} \Pi_{\uparrow} & \sigma_{\downarrow} \Pi_{\downarrow} & k \end{pmatrix} \cdot \begin{pmatrix} \nabla \mu_{\uparrow} / e \\ \nabla \mu_{\downarrow} / e \\ \nabla T \end{pmatrix}$$



# Magnonic Spin-Transfer Torque MRAM With Low Power, High Speed, and Error-Free Switching

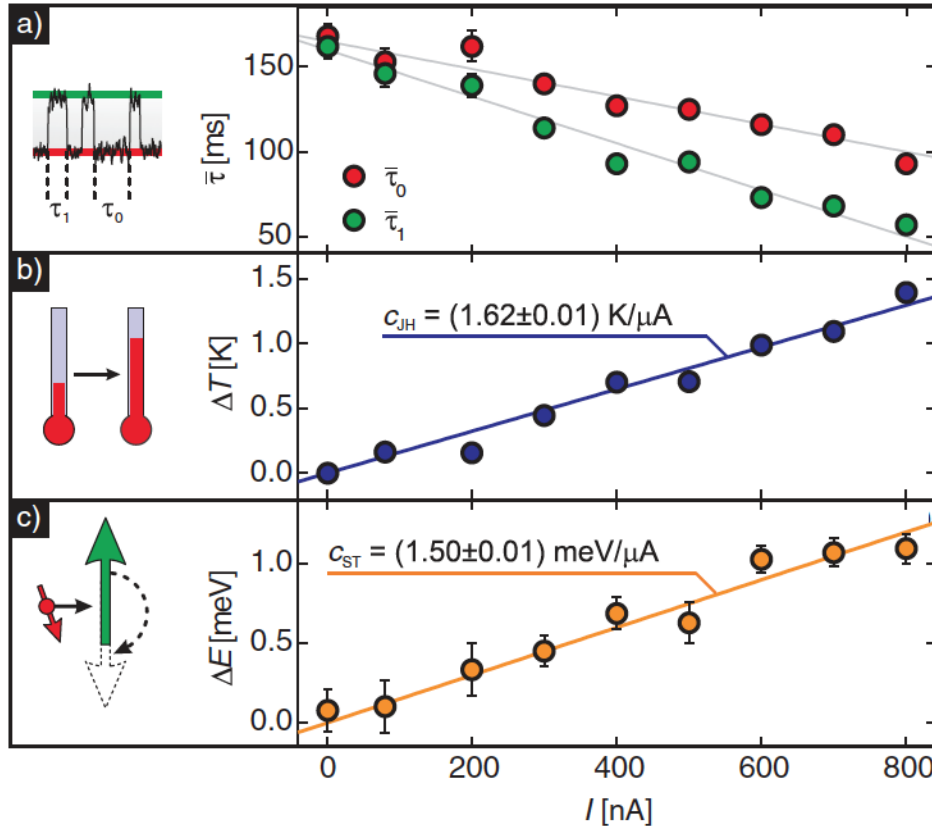
Niladri N. Mojumder<sup>1,2</sup>, David W. Abraham<sup>1</sup>, Kaushik Roy<sup>2</sup>, and D. C. Worledge<sup>1</sup>





# Joule Heating and Spin-Transfer Torque Investigated on the Atomic Scale Using a Spin-Polarized Scanning Tunneling Microscope

S. Krause,\* G. Herzog, A. Schlenhoff, A. Sonntag, and R. Wiesendanger

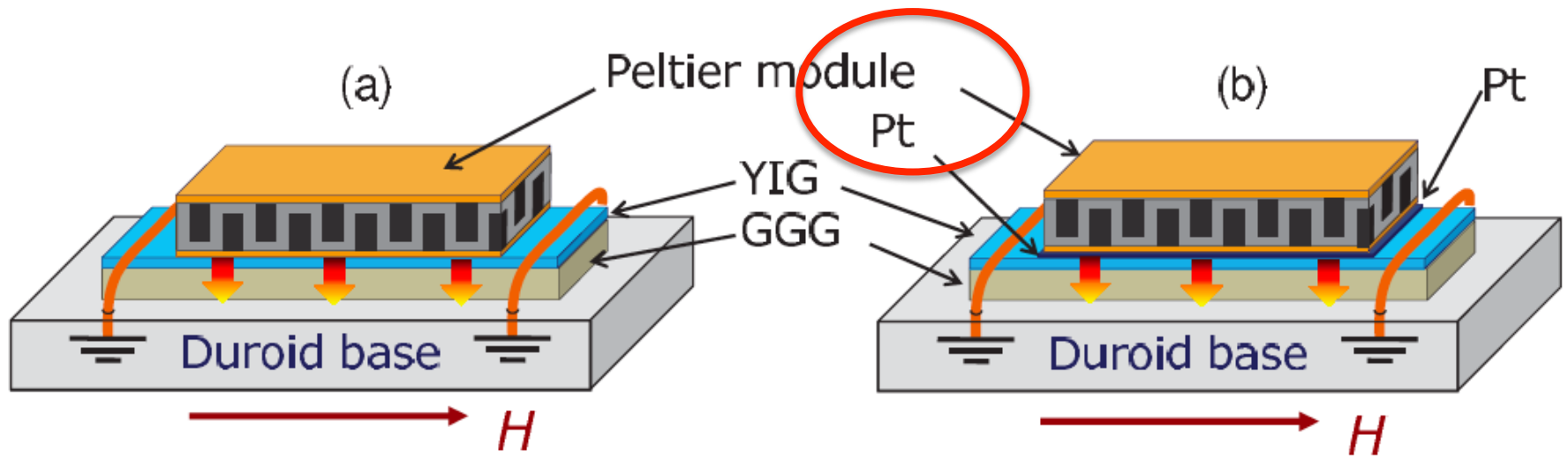


$$\bar{\tau}_{0,1}(I) = \frac{1}{f_0} \exp\left(\frac{E_b \pm \Delta E(I)}{k_B[T + \Delta T(I)]}\right)$$

2 data series

# Controlling the relaxation of propagating spin waves in yttrium iron garnet/Pt bilayers with thermal gradients

R. O. Cunha, E. Padrón-Hernández, A. Azevedo, and S. M. Rezende\*



**H and grad T are perpendicular :**

- no Pt : no effect (ok with our experiment)
- with Pt : damping depends on the sign of the gradient



# Magnetization dynamics under heat current

- Thermodynamics with  $P$  and  $M$  as state fields
- **Magnetic Seebeck effect :**  
out-of-phase  $B$  field induced by temperature gradient  
when  $M$  *out of equilibrium*
- Heat-driven spin currents in metals :
  - Switching assisted by heat-driven spin current
  - AC voltage due to AC heat-driven spin torque  
when DC current is applied

